

# Inequality, Costly Redistribution and Welfare in an Open Economy

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## Introduction

- International trade raises real income but also increases inequality and makes some worse off
- Standard approach to demonstrating and quantifying the gains from trade largely ignore trade-induced inequality
  - Kaldor-Hicks compensation principle
- Two issues with this approach:
  - ① How much compensation/redistribution **actually** takes place?
  - ② Is this redistribution **costless**, as the Kaldor-Hicks approach assumes?
- These issue are relevant not just for trade, but also for any change with redistributive effects (e.g., technological change)

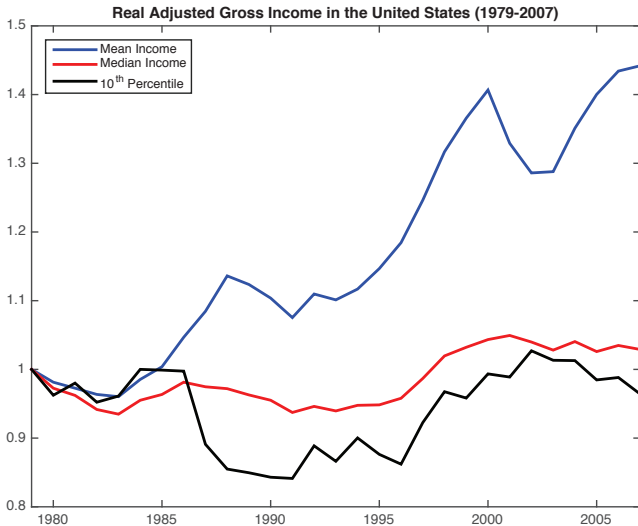
## This Paper

- We study quantitatively welfare implications of trade in a model where:
  - ① trade leads to an increase in inequality
  - ② redistribution requires distortionary taxation (e.g., due to informational constraints, as in Mirrlees)
  - ③ despite progressive tax system, trade still increases inequality in after-tax incomes

## This Paper

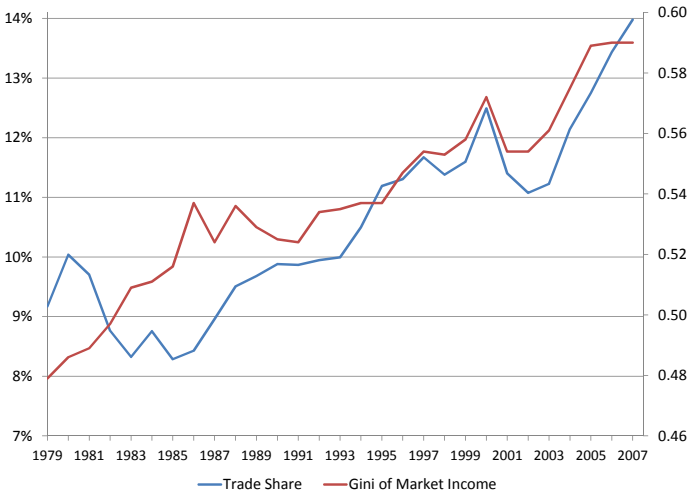
- We study quantitatively welfare implications of trade in a model where:
  - ① trade leads to an increase in inequality
  - ② redistribution requires distortionary taxation (e.g., due to informational constraints, as in Mirrlees)
  - ③ despite progressive tax system, trade still increases inequality in after-tax incomes
- We propose two types of adjustment to standard welfare measures:
  - ① **Welfarist correction**: taking into account inequality-aversion of society (or risk-adjustment under the veil of ignorance)
  - ② **Costly-redistribution correction**: capturing behavioral responses to *trade-induced* shifts across marginal tax rates

## Two Motivating Figures



## Two Motivating Figures

Openness and Inequality in the United States (1979-2007)



## Building Blocks

- Skeleton of Trade Model: Itskhoki (2009)
  - Melitz (2003) with heterogeneous worker-entrepreneurs
  - endogenous labor supply decision with a constant elasticity
- Costly Redistribution: nonlinear progressive tax system
  - after-tax income is log-linear function of pre-tax income
  - Benabou (2002), Heathcote, Storesletten and Violante (2014)
- Constant degree of inequality-aversion
  - widely used in Public Finance (Atkison 1970)
  - equivalent to risk-aversion behind the veil of ignorance
- Model calibrated to fit 2007 U.S. data:
  - distribution of skills calibrated to match U.S. distribution of (adjusted gross) income from IRS public records
  - trade costs calibrated to match the key U.S. trade moments

## Other Related Literature

- Trade models with heterogeneous workers:
  - matching/sorting models (see Grossman and Costinot and Vogel for surveys)
  - models with imperfect labor markets (e.g., Helpman, Itskhoki, Redding, and earlier Davidson and Matusz)
- Gains from trade and costly redistribution:
  - Dixit and Norman (1986)
  - Rodrik (1992), Spector (2001), Naito (2006)
- Old literature on Kaldor-Hicks:
  - Kaldor (1939), Hicks (1939), Scitovszky (1941)
- Welfarist approach:
  - Bergson (1938), Samuelson (1947)
  - Diamond & Mirlees (1971), Saez (2003, 2004)
- Costly-redistribution: Kaplow (2008), Hendren (2014)



# Road Map

## ① Motivating Example

- Kaldor-Hicks
- Welfarist correction
- Costly-redistribution correction

## ② Constant-Elasticity Model

- A preliminary look at the data

## ③ Open Economy Model

- Calibration
- Counterfactuals: inequality and the gains from trade

# MOTIVATING EXAMPLE

## The Kaldor-Hicks Principle

- Consider an economy with a unit measure of individuals with ability  $\varphi \sim H_\varphi$  earning market income  $r_\varphi \sim F_r$
- We want to evaluate a **shift of income distribution**  $F_r \rightarrow F'_r$

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$$u(r_\varphi) = u(r'_\varphi + v_\varphi) \quad \Rightarrow \quad v_\varphi = r_\varphi - r'_\varphi$$

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- Hence:

$$\begin{aligned} - \int v_\varphi dH_\varphi &= \int r'_\varphi dH_\varphi - \int r_\varphi dH_\varphi \\ &= \int r dF'_r - \int r dF_r = R' - R \end{aligned}$$

- Kaldor-Hicks Gains = Aggregate Real Income Growth

$$G^{KH} = \frac{R' - R}{R} \equiv \mu$$

# The Kaldor-Hicks Principle

## Pros and Cons

- Principle does not rely on interpersonal comparisons of utility:
  - indirect utility can be heterogeneous across agents
  - result relies on ordinal rather than cardinal preferences
  - notion of efficiency argued to be free of value judgements
- What if redistribution does not take place?
  - under the veil of ignorance, agents see a probability distribution over potential outcomes (need cardinal preferences)
  - risk aversion  $\approx$  inequality aversion
- Even if some redistribution takes place, whenever it is costly, shouldn't  $\Delta W/W$  reflect those costs?
  - Dixit and Norman (1986) showed that  $\Delta W/W > 0$  using a course set of taxes, but by how much is  $\Delta W/W$  diminished?

## Welfarist Correction

- Social Welfare Function:  $V = \int g(r_\varphi^d) dH_\varphi$
- Constant inequality aversion:  $g(r) = \frac{r^{1-\rho}-1}{1-\rho}$
- Convenient transformation:  $W = \left[1 + (1 - \rho)V\right]^{\frac{1}{1-\rho}}$

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- Convenient transformation:  $W = \left[1 + (1 - \rho)V\right]^{\frac{1}{1-\rho}}$
- Welfare can be represented:

$$W = \Delta \times R, \quad \Delta \equiv \Delta(F_r^d; \rho) = \frac{\left[\mathbb{E}(r_\varphi^d)^{1-\rho}\right]^{\frac{1}{1-\rho}}}{\mathbb{E}r_\varphi^d} \leq 1$$

- Welfare gains:  $G^W = (1 + \mu) \frac{\Delta'}{\Delta} - 1$



## Costly-Redistribution Correction

- Disposable after-tax income:  $r_\varphi^d = [1 - \tau(r_\varphi)]r_\varphi + T_\varphi$
- No lump-sum taxes and tax schedule:  $r_\varphi^d = kr_\varphi^{1-\phi}$
- Marginal tax rate:  $\tau_m(r_\varphi) = 1 - k(1 - \phi)r_\varphi^{-\phi}$
- Constant behavioral elasticity:  $\varepsilon \equiv \frac{\partial \log r_\varphi}{\partial \log (1 - \tau_m(r_\varphi))} \geq 0$
- Counterfactual no-tax income:  $\tilde{r}_\varphi = (1 - \phi)^{-\varepsilon} r_\varphi^{1+\varepsilon\phi}$

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- Aggregate income loss:

$$R = \Theta \times \tilde{R}, \quad \Theta \equiv \Theta(F_r; \varepsilon, \phi) = (1 - \phi)^\varepsilon \frac{(\mathbb{E}r_\varphi)^{1+\varepsilon}}{(\mathbb{E}r_\varphi^{1-\phi})^\varepsilon \cdot (\mathbb{E}r_\varphi^{1+\varepsilon\phi})}$$

- Aggregate income gains:  $\mu = (1 + \tilde{\mu}) \frac{\Theta'}{\Theta} - 1$

## Two Correction Together

- We have:

$$W = \Delta(F_r^d; \rho) \times R \quad \text{and} \quad R = \Theta(F_r; \varepsilon, \phi) \times \tilde{R},$$

and  $r_\varphi^d = kr_\varphi^{1-\phi}$

- Comparative statics:
  - ①  $\Delta$  declines with  $\rho$ ;  $\Theta$  declines with  $\phi$  and  $\varepsilon$
  - ②  $\Delta$  and  $\Theta$  decline with the dispersion of  $r_\varphi^d$  and  $r_\varphi$ , respectively
  - ③ Higher  $\phi$  reduces dispersion in  $r_\varphi^d \rightarrow$  policy tradeoff

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- Parametric Example (log-normal):

$$\Delta = e^{-\rho(1-\phi)^2 \frac{\sigma^2}{2}} \quad \text{and} \quad \Theta = (1-\phi)^\varepsilon e^{-\varepsilon(1+\varepsilon)\phi^2 \frac{\sigma^2}{2}}$$

$$\text{where } \sigma^2 = \frac{1}{(1+\varepsilon\phi)^2} \tilde{\sigma}^2 \quad \text{and} \quad \text{Gini} = 2\Phi(\sigma/\sqrt{2}) - 1$$

— similar results with Pareto

# CONSTANT-ELASTICITY MODEL

# A Constant-Elasticity Model

Closed Economy

- A unit measure of individuals with CRRA-GHH utility:

$$U(c, \ell) = \frac{1}{1-\rho} \left( c - \frac{1}{\gamma} \ell^\gamma \right)^{1-\rho}$$

- Each individual produces a task according to  $y = \varphi \ell$ ,  $\varphi \sim H_\varphi$
- This translates into market income

$$r = Q^{1-\beta} y^\beta, \quad Q = R = \int r_\varphi dH_\varphi$$

- Consumption equals after-tax income:

$$c = r - T(r) = kr^{1-\phi},$$

government runs balanced budget (finances expenditure  $gQ$ )

# A Constant-Elasticity Model

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- In constant-elasticity model:  $r_\varphi \propto \varphi^{\frac{\beta(1+\varepsilon)}{1+\varepsilon\phi}}$

— two auxiliary parameters:  $\varepsilon \equiv \frac{\beta}{\gamma-\beta}$  and  $\kappa \equiv \frac{1}{1-(1-\beta)(1+\varepsilon)}$

## Theoretical Welfare Corrections

- Welfare:

$$W = \Delta \times \hat{\Theta} \times \tilde{W}, \quad \text{where} \quad \tilde{W} = \frac{1 - g}{1 + \varepsilon} \tilde{R}$$

- Welfarist Correction:

$$\Delta \equiv \frac{\left( \int r_{\varphi}^{(1-\phi)(1-\rho)} dH_{\varphi} \right)^{\frac{1}{1-\rho}}}{\int r_{\varphi}^{1-\phi} dH_{\varphi}}$$

- Costly Redistribution Correction:

$$\hat{\Theta} \equiv (1 + \varepsilon \phi) \frac{R}{\tilde{R}} = \underbrace{(1 + \varepsilon \phi)(1 - \phi)^{\kappa \varepsilon}}_{\equiv \tilde{\Theta}} \left[ \underbrace{\frac{\left( \int r_{\varphi} dH_{\varphi} \right)^{1 + \varepsilon}}{\left( \int r_{\varphi}^{1-\phi} dH_{\varphi} \right)^{\varepsilon} \int r_{\varphi}^{1 + \varepsilon \phi} dH_{\varphi}}}_{\equiv \tilde{\Theta}} \right]^{\kappa}$$



# FIRST LOOK AT THE DATA

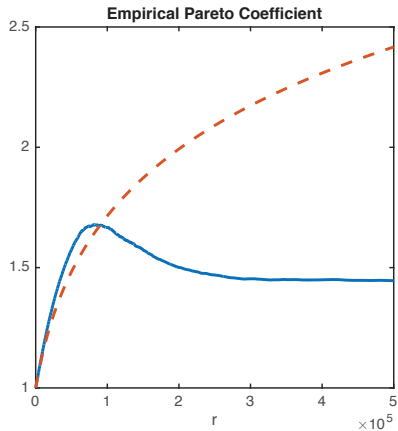
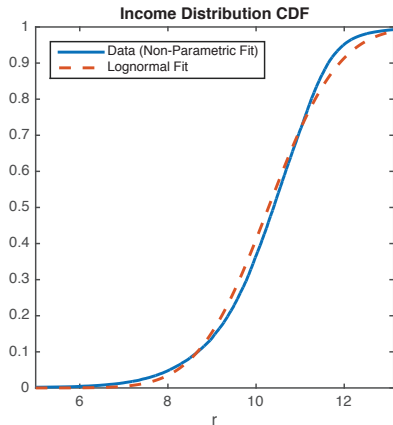
# Calibration

## U.S. Income Growth (1979-2007)

- Use U.S. Individual Income Tax Public Use Sample to calibrate distribution of market income
  - approximately 3.5 million anonymized tax returns
  - use NBER weights to ensure this is a representative sample
  - we map market income to adjusted gross income in line 37 of IRS Form 1040
- Use CBO data on before-tax and after-tax/transfer income to calibrate the degree of tax progressivity  $\phi$
- Elasticity of substitution = 5 ( $\beta = 4/5$ )
- Experiment with various values of  $\varepsilon$  and  $\rho$ 
  - benchmark  $\varepsilon = 0.5$  and  $\rho = 1$

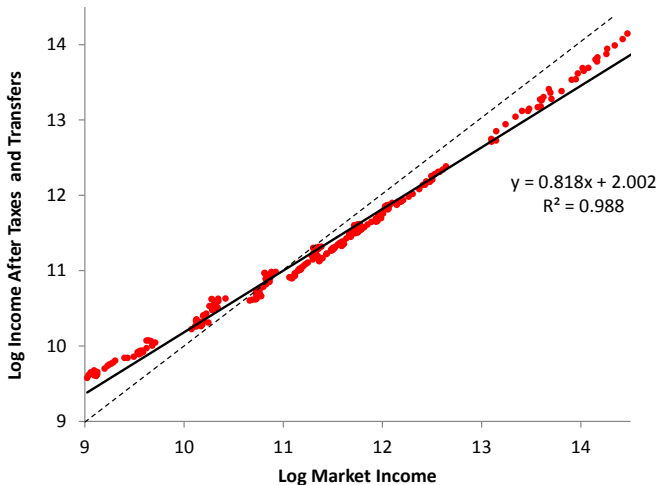
## Income Distribution

- Log-normal provides a good approximation, but it does a poor fit for the right-tail of the distribution, which looks Pareto



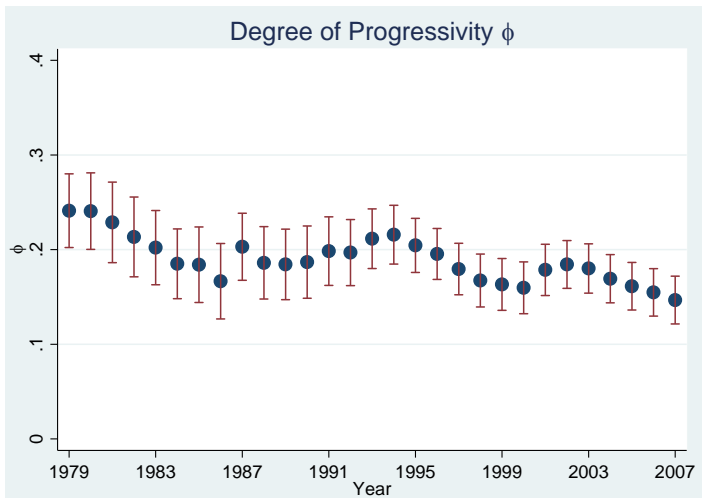
## Tax Progressivity

- Tax schedule  $r^d = kr^{1-\phi}$  may seem ad hoc, but it fits U.S. data remarkably well (similar fit with PSID data)



## Tax Progressivity Over Time

- Tax schedule  $r^d = kr^{1-\phi}$  may seem ad hoc, but it fits U.S. data remarkably well (similar fit with PSID data)



## Counterfactuals: 1979–2007

- Mean real income grew 44.2%, or **1.32%** per year
- For the logarithmic case ( $\rho = 1$ ), the implied annual growth rate in social welfare is only **0.31%**
  - partly due to the observed decline in progressivity

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- *By how much would real income and social welfare have increased if  $\phi$  had been held constant at its 1979 level?*

For  $\rho = 1$  and  $\varepsilon = 0.5$ :

- mean real income by **0.90%** per year
- social welfare by **0.52%** per year

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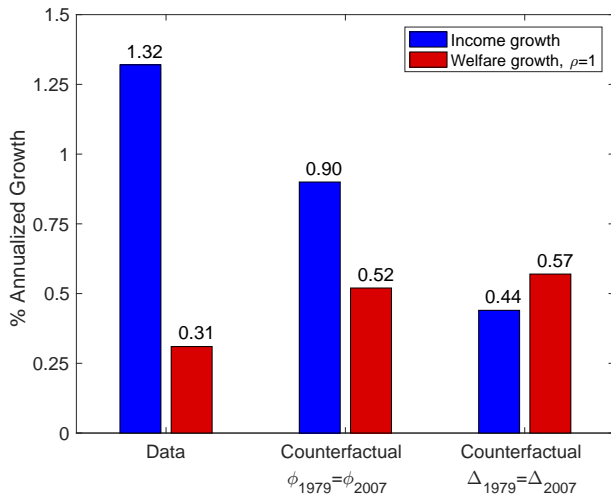
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- mean real income by **0.90%** per year
- social welfare by **0.52%** per year
- *By how much would real income and social welfare have increased if  $\phi$  had kept  $\Delta$  at its 1979 level?*
  - mean real income by **0.44%** per year
  - social welfare by **0.57%** per year

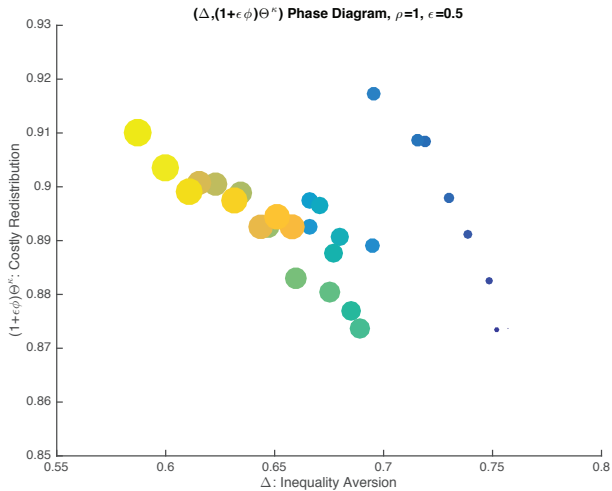


# Social Welfare and Counterfactuals



▶ show  $\rho = 0.5$

# Evolution of Welfare Corrections



# OPEN ECONOMIC MODEL

# Open Economy

## Environment

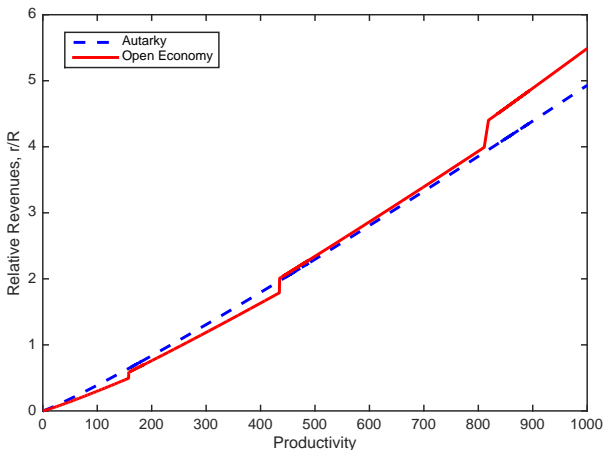
- Consider a world economy with  $N + 1$  symmetric regions
- Households can market their output (task) locally or in any of the other  $N$  regions
- Trade/Offshoring involves two types of additional costs
  - ① Variable iceberg trade cost  $\tau$
  - ② Fixed cost of market access  $f(n)$  increasing in the number  $n$  of foreign markets served. We adopt  $f(n) = fn^\alpha$
- Household income

$$r_\varphi = \Upsilon_{n_\varphi}^{1-\beta} Q^{1-\beta} y_\varphi^\beta, \quad \text{where} \quad \Upsilon_{n_\varphi} = 1 + n_\varphi \tau^{-\frac{\beta}{1-\beta}}$$

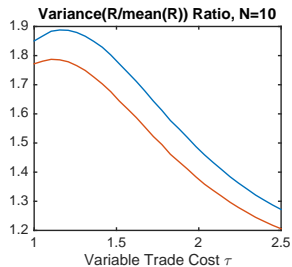
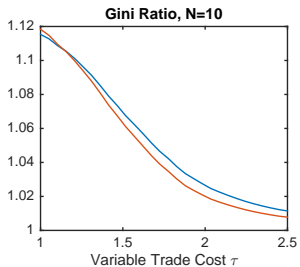
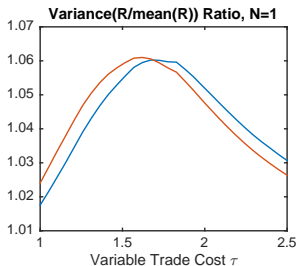
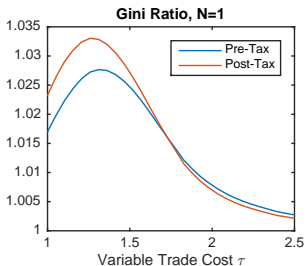
- Taxation: the government does not observe export decisions and  $f(n)$  is not tax deductible:  $c_\varphi = kr_\varphi^{1-\phi} - \sum_{n=1}^{n_\varphi} fn^\alpha$

## Trade and Inequality

- Trade increases relative revenues of high-ability households (due to market access), but reduces that of low-ability households (due to foreign competition)



# Trade and Inequality



# CALIBRATION AND COUNTERFACTUALS

## Calibration and Counterfactuals

- We first calibrate the model to 2007 U.S. data
  - as in the closed economy but with additional trade moments
- We then explore the implication of a move to the 1979 level of trade openness (and to autarky) on:
  - ① Aggregate Income
  - ② Income Inequality
- We use the model to gauge the quantitative importance of the two corrections developed above

$$W = \frac{\left[ \mathbb{E}(u_\varphi)^{1-\rho} \right]^{\frac{1}{1-\rho}}}{\mathbb{E}u_\varphi} \times \frac{\mathbb{E}u_\varphi}{\tilde{W}} \times \tilde{W} = \Delta_T \times \Theta_T \times \tilde{W}.$$

- ① How large is  $W'/W$  for different degrees of inequality aversion?
- ② How large would  $W'/W$  be in the absence of costly redistribution?



## Calibration

- For our benchmark results, hold the following primitives constant:
  - ① As in closed economy, set  $\beta = 4/5$  and  $\gamma = 2.4 \Rightarrow \varepsilon = 0.5$
  - ② Tax progressively  $\phi = 0.147$  for 2007
  - ③ Number of countries  $N = 5$  (i.e., US roughly 15% of the world)
- Jointly calibrate trade parameters  $(\tau, f_x, \alpha)$  and the ability distribution  $H_\varphi$  to match:
  - ① 2007 trade share of 7.8% from NIPA  $\Rightarrow \tau = 2.11$
  - ② Share of exporter sales in total sales = 60%  $\Rightarrow f_x = \$750$
  - ③ Skewness of export sales: firms that export to  $n > 1$  dest. account for 89% of total exporters' sales  $\Rightarrow \alpha = 0.53$
  - ④ The 2007 distribution of market income from the IRS data  
▶ Implied  $H_\varphi$
- In the counterfactuals, we then set  $\tau_{1979} = 2.25$  to match 1979 trade share of 5.2% (holding all else equal); also  $\tau_A = \infty$

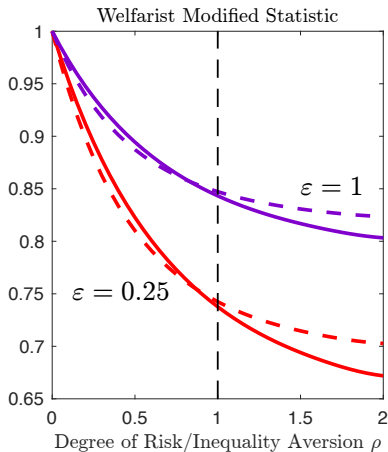
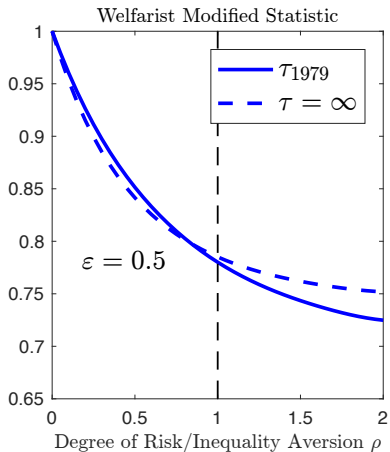
## Calibrated Welfare Gains from Trade and Inequality

- Calibrated welfare gains from trade are higher, the higher is the labor supply elasticity  $\varepsilon$  (Arkolakis and Esposito, 2014)
- But relative to autarky trade induces more inequality when  $\varepsilon$  is high

	% Consumption Gains		% Welfare Gains ( $\rho = 0$ )		% Increase in Gini	
	$\tau_{1979}$	$\tau = \infty$	$\tau_{1979}$	$\tau = \infty$	$\tau_{1979}$	$\tau = \infty$
$\varepsilon = 0.25$	0.8	2.5	0.8	2.4	0.4	1.1
$\varepsilon = 0.5$	1.2	3.5	1.1	3.3	0.5	1.3
$\varepsilon = 1$	2.0	6.3	1.8	5.9	0.6	1.7

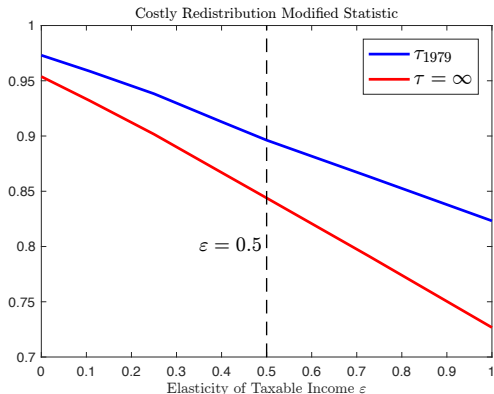
## Welfarist Correction

- Welfarist correction is higher, the higher is  $\rho$  and the lower is  $\varepsilon$
- With log utility ( $\rho = 1$ ) and a labor supply elasticity of  $\varepsilon = 0.5$ , welfare gains are 21% lower



## Costly Redistribution Correction

- Costly redistribution correction is higher, the higher is  $\varepsilon$
- When  $\varepsilon = 0.5$ , welfare gains are 10% lower (when moving to  $\tau_{1979}$ ) and 16% lower (when moving to autarky)



## Robustness and Additional Exercises

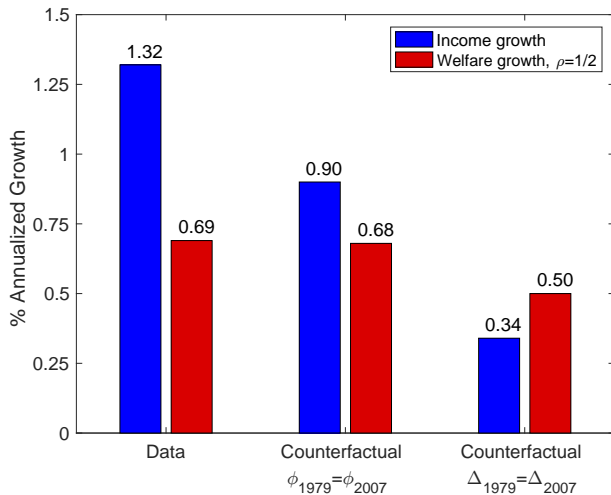
- Imposing a lognormal distribution of income **underpredicts** costly redistribution correction ▶ Lognormal
- Allowing for progressivity to endogenously adjust to trade opening makes little difference ▶ Endogenous  $\phi$
- The size of the corrections is fairly robust to:
  - Alternative values of  $\beta$ , holding constant  $\varepsilon$  ▶ Different  $\beta$
  - Alternative values of the share of exporter sales in total sales
  - Setting  $\alpha = 0$  as in Melitz (2003)
  - Calibrating trade costs  $(\tau, F, \alpha)$  to the manufacturing sector

## Conclusions

- Trade-induced inequality is partly mitigated via a progressive income tax system
- Still, compensation is not full so trade induces an increase in the inequality of disposable income
  - should we measure gains using average income or adjust for inequality?
- Income taxation induces behavioral responses that affect the aggregate income response to trade integration
  - should we adjust for this “leaky bucket” effect?
- We developed welfarist and costly redistribution corrections to standard measures of the gains from trade
- Under plausible parameter values, these corrections are nonnegligible and eliminate about one-fifth of the gains

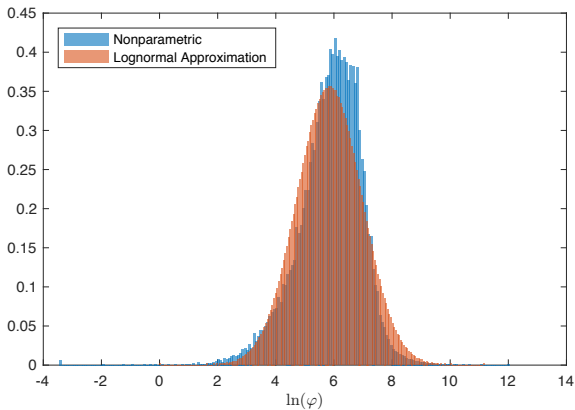
# APPENDIX

# Social Welfare and Counterfactuals





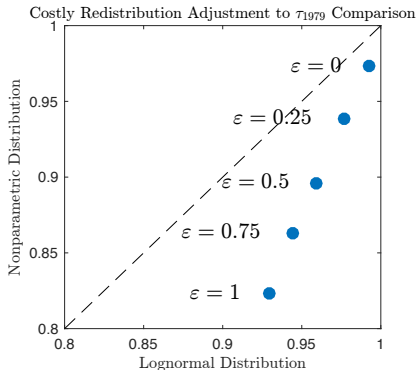
## Implied 2007 Ability Distribution $H_\varphi$



◀ back to slides

## Nonparametric versus Lognormal Case

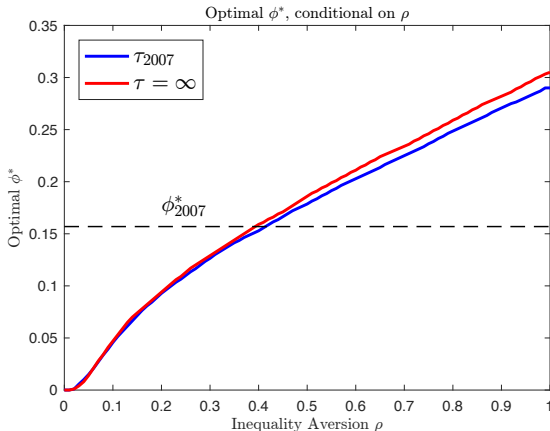
- Lognormal **underpredicts** costly redistribution correction, esp. for high  $\varepsilon$  (underpredicts the behavior of the right tail)



# Optimal Progressivity

(and Implied Inequality Aversion)

- Observed degree of progressivity in 2007 is optimal if  $\rho$  is relatively low; optimal  $\phi$  with trade is very similar



## Alternative Values of $\beta$ (constant $\varepsilon$ )

